

**International Conference on Mathematics
and Computer Science
4th Edition - MACOS 2022**

Braşov, September 15-17, 2022

Contents

Technical Program	1
Abstracts	9
Combinatorial optimization interdiction problems with linear costs (<i>Javad Tayyebi</i>)	9
Semilocal Approximation an some popular Diophantine equations (<i>Preda Mihăilescu</i>)	9
Inevitable remarks on some recent results in metric fixed point theory (<i>Erdal Karapınar</i>)	10
Successive coefficients of close-to-convex functions (<i>Paweł Zaprawa</i>)	10
On Marx-Strohhäcker type results for multivalent functions and their n^{th} root (<i>Dorina Răducanu</i>)	11
Logarithmic coefficients for a class of analytic functions defined by subordination (<i>Andreea Nistor-Șerban and Dorina Răducanu</i>)	11
Some new characterizations of inner product spaces regarding the p -angular distance (<i>Mario Krnić (joint work with Nicușor Minculete)</i>)	12
Asymptotic expansions of stable means (<i>Lenka Mihoković</i>)	12
Comparison of exact and heuristic method for numerical approximation of functions (<i>Tomislav Burić</i>)	13
Redistributing algorithms and Shannon's Entropy: how to redistribute the ties? (<i>Flavia-Corina Mitroi-Symeonidis and Eleutherius Symeonidis</i>)	13
On the Space of Homogeneous Modified Harmonic Polynomials (<i>Eleutherius Symeonidis</i>)	14
Estimates of approximation using higher order moduli of continuity (<i>Radu Păltănea</i>)	14
Several inequalities related to the numerical radius (<i>Nicușor Minculete</i>)	15
Energy drift and stochastic process in the three-body problem (<i>Marian Gîdea</i>)	15
About some speeds of convergence to the the constant of Euler (<i>Andrei Vernescu</i>)	15
On approximation properties of some non-positive Bernstein-Durrmeyer type operators modified in the Bezier-King sense (<i>Bianca Vasian</i>)	16
On the convergence of power series of positive linear operators (<i>Ștefan Garoiu and Radu Păltănea</i>)	16
The 3-convexity flavor of the Hornich-Hlawka inequality (<i>Constantin P. Niculescu</i>)	17

End-to-end data privacy using homomorphic encryption models (<i>Răzvan Bocu and Delia Monica Duca Iliescu</i>)	17
Mammographic texture analysis in the diagnosis of breast cancer (<i>Andreea-Bianca Lixandru, Laura Dioşan and Mircea-Lucian Sasu</i>)	18
Advances in CUDA for Computational Physics (<i>Delia Spridon</i>)	18
Image processing in medicine: the algorithms and datasets for searching the spatial location of brain intracranial aneurysms (<i>Sergey Sinitsa</i>)	19
Fixed Point Theory for Abstract Volterra Operators (<i>Adrian Petruşel</i>)	19
Interpolation type iterated function systems (<i>Radu Miculescu</i>)	19
Fixed points of interpolative contractions (<i>İsa Yildirim, Y. Serdar Sahin</i>)	20
A countable fractal interpolation scheme involving Rakotch contractions (<i>Cristina Păcurar</i>)	20
Some remarks on convex orbital operators (<i>Ovidiu Popescu</i>)	20
The approximation of controls using moment problems (<i>Ionel Roventă and József Kolumbán</i>)	21
A study on the Research Directions of some Cesàro and Rhaly Operators (<i>Amelia Bucur , María del Carmen Listán - García and María del Pilar Romero-De La Rosa</i>)	21
Fixed point theory for multi-valued nonlinear graph contractions in complete metric spaces (<i>Mădălina Moga , Adrian Petruşel, Radu Truşcă</i>)	22
Some fixed point theorems in the framework of f -metric spaces (<i>Bogdan-Cristian Anghelina</i>)	22
φ - Contractive Orbital Affine Iterated Function Systems (<i>Irina Savu</i>)	23
An application of Edelstein's contraction principle: the attractor of a graph-directed generalized iterated function system (<i>Radu Miculescu, Alexandru Mihail and Silviu-Aurelian Urziceanu</i>)	23
About the B-concavity of functions with many variables (<i>Alexandra-Diana Melesteu</i>)	23
Fixed point theorems on product of b -metric spaces (<i>Izabella Abraham</i>)	24
On the solutions of several coupled systems of fractional differential inclusions (<i>Aurelian Cernea</i>)	24
Fractional q -difference Schrödinger equations with integral and multi-point boundary conditions (<i>Umit Aksoy</i>)	24
Nonlinear Diffusion-based Image Edge Detection Solutions (<i>Tudor Barbu</i>)	25
On the existence and uniqueness of solutions of fractional dynamic equations on time scales (<i>Inci Erhan</i>)	26
On the Mersenne Hybrinomial Quaternions (<i>Engin Özkan, Bahar Kuloğlu and Engin Eser</i>)	26
On Mersenne Hybrid Quaternions (<i>Engin Özkan and Mine Uysal</i>)	26
Division quaternion algebras over extensions of degree l^n (where l is an odd prime integer) of quadratic number fields (<i>Diana Savin (joint work with Vincenzo Acciari, Mohammed Taous and Abdelkader Zekhnini)</i>)	27
Surfaces associated with Pascal and Catalan triangles (<i>Adela Mihai</i>)	27
Cosmological Finsler Spacetimes (<i>Nicoleta Voicu, Manuel Hohmann and Christian Pfeifer</i>)	28

Methods Used to Extract the Photovoltaic Cells and Panel Parameters (<i>Adrian-Marius Deaconu</i>)	28
Credentials are the holy grail for hackers (<i>Cristina-Alexandra Caldarea,</i> <i>Silviu-Razvan Dumitrescu</i>)	29
An Incremental Minimum Flow Algorithm (<i>Luciana Majercsik</i>)	29
Bottleneck spanning tree interdiction problem with fixed and linear costs (<i>Abolfazl Abdolazadeh, Massoud Aman, Javad Tayyebi</i>)	29
Spatial behaviour in the coupled theory of viscoelasticity of porous mate- rials (<i>Adina Chirilă</i>)	30
Existence of solutions for a variational relation problem (<i>Mircea Balaj</i> <i>and Dan Florin Serac</i>)	30
Some results for isotropic micropolar bodies with pores (<i>Iana M. Fudulu</i> <i>and Marin Marin</i>)	30
Inside Neural Networks (<i>Detlef Streitferdt</i>)	31

Author Index **33**

Technical Program

September 15, 2022

14:30 - 15:30 Registration of participants

Transilvania University Hall– *Iuliu Maniu nr. 41A*

15:30 - 15:45 Opening Ceremony and group photo

Transilvania University Hall

16:00-18:40 Plenary session

Transilvania University Hall

Chair: Dorina Răducanu

16:00-16:50 Combinatorial optimization interdiction problems with linear costs
Javad Tayyebi

16:50-17:10 Coffee Break

17:10-18:40 Semilocal Approximation an some popular Diophantine equations
Preda Mihăilescu

18:45-19:15 Musical moment

19:30 Welcome Cocktail

September 16, 2022

9:00-9:50 Plenary session

Chair: Adrian Petrușel

9:00-9:50 Inevitable remarks on some recent results in metric fixed point theory
Erdal Karapinar

Transilvania University Hall

10:00-11:20 Mathematical Analysis (UI6 Room)

Chair: Radu Păltănea

10:00-10:20 Successive coefficients of close-to-convex functions
Pawel Zaprawa

10:20-10:40 On Marx-Strohhacker type results for multivalent functions
Dorina Răducanu

10:40-11:00 Logarithmic coefficients for a class of analytic functions defined by subordination
Andreea Nistor-Șerban and Dorina Răducanu

11:00-11:20 Some new characterizations of inner product spaces regarding
the p -angular distance
Mario Krnić

11:20-11:30 Coffee Break

11:30-13:30 Mathematical Analysis (UI6 Room)

Chair: Mario Krnić

11:30-11:50 Asymptotic expansions of stable means
Lenka Mihoković

11:50-12:10 Comparison of exact and heuristic methods for numerical approximation
of functions
Tomislav Burić

12:10-12:30 Redistributing algorithms and Shannon's Entropy: how to redistribute the ties?
Flavia-Corina Mitroi-Symeonidis and Eleutherius Symeonidis

12:30-12:50 On the Space of Homogeneous Modified Harmonic Polynomials
Eleutherius Symeonidis

12:50-13:10 Estimates of approximation using higher order moduli of continuity
Radu Păltănea

13:10-13:30 Several inequalities related to the numerical radius
Nicușor Minculete

13:30 - 15:30 Lunch ("Casa Romaneasca" Restaurant – Piața Unirii 15)

15:30-16:20 Plenary session

Chair: Adrian Petrușel

15:30-16:20 Energy drift and stochastic process in the three-body problem
Marian Gîdea

Transilvania University Hall

16:30-19:20 Mathematical Analysis (UI6 Room)

Chair: Nicușor Minculete

16:30-16:50 About some speeds of convergence to the constant of Euler
Andrei Vernescu

16:50-17:10 On approximation properties of some non-positive Bernstein-Durrmeyer type operators
Bianca Vasian

17:10-17:30 On the convergence of power series of positive linear operators
Ștefan Garoiu, Radu Păltănea

17:30-17:50 The 3-convexity flavor of the Hornich-Hlawka inequality
Constantin Niculescu

17:50-18:00 Coffee Break

Chair: Adrian Marius Deaconu

18:00-18:20 End-to-end data privacy using homomorphic encryption models
Razvan Bocu, Delia Monica Duca Iliescu

18:20-18:40 Mammographic texture analysis in the diagnosis of breast cancer
Andreea-Bianca Lixandru, Laura Dioșan, Mircea-Lucian Sasu

18:40-19:00 Advances in CUDA for Computational Physics
Delia Spridon

19:00-19:20 Image processing in medicine: the algorithms and datasets for searching the spatial location of brain intracranial aneurysms
Sergey Sinitza

10:00-11:20 Mathematical Analysis (UI3 Room)

Chair: Ionel Roventța

10:00-10:20 Fixed point theory for abstract Volterra operators
Adrian Petrușel

- 10:20-10:40 Interpolation type iterated function systems
Radu Miculescu
- 10:40-11:00 Interpolative Contractions in Convex b -Metric Spaces
Isa Yldirim, Y. Serdar Sahin
- 11:00-11:20 A Countable Fractal Interpolation Scheme Involving Rakotch Contractions
Cristina Maria Păcurar

11:20-11:30 Coffee Break

11:30-13:30 Mathematical Analysis (UI3 Room)

Chair: Erdal Karapinar

- 11:30-11:50 Some remarks on convex orbital operators
Ovidiu Popescu
- 11:50-12:10 The approximation of controls using moment problems
Ionel Roventă and József Kolumbán
- 12:10-12:30 A study on the research directions of some Cesaro and Rhaly operators
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Mădălina Moga, Radu Trușcă
- 12:50-13:10 Some fixed point theorems in the framework of f -metric spaces
Bogdan-Cristian Anghelina
- 13:10-13:30 On the Connectedness of Attractors of Orbital Contractive IFSs
Maria-Irina Savu

16:30-19:20 Mathematical Analysis (UI3 Room)

Chair: Radu Miculescu

- 16:30-16:50 An application of Edelstein's contraction principle: the attractor of a graph-directed generalized iterated function system
Radu Miculescu, Alexandru Mihail, Silviu-Aurelian Urziceanu
- 16:50-17:10 About the B-concavity of functions with many variables
Alexandra Diana Meleşteu

17:10-17:30 Fixed point theorems on product of b -metric spaces
Izabella Abraham

17:50-18:00 Coffee Break

10:00-11:20 Applied Mathematics and Computer Science (UI2 Room)

Chair: Marian Gîdea

10:00-10:20 On the solutions of several coupled systems of fractional differential inclusions
Aurelian Cernea

10:20-10:40 Fractional q -difference Schrödinger equations with integral and multi-point boundary conditions
Ümit Aksoy

10:40-11:00 Nonlinear Diffusion-based Image Edge Detection Solutions
Tudor Barbu

11:00-11:20 Existence and uniqueness of solutions of fractional dynamic equations
Inci Erhan

11:20-11:30 Coffee Break

11:30-13:30 Algebra and Geometry (UI2 Room)

Chair: Preda Mihăilescu

11:30-11:50 On the Mersenne Hybrinomial Quaternions
Engin Özkan, Bahar Kuloğlu, Engin Eser

11:50-12:10 On Mersenne Hybrid Quaternions
Engin Özkan, Mine Uysal

12:10-12:30 Division quaternion algebras over extensions of degree l^n of quadratic number fields, where l is an odd prime integer
Savin Diana

12:30-12:50 Surfaces Associated with Pascal and Catalan Triangles
Adela Mihai

12:50-13:10 Cosmological Finsler Spacetimes
Nicoleta Voicu, Manuel Hohmann, Christian Pfeifer

16:30-19:20 Applied Mathematics and Computer Science (UI2 Room)

Chair: Javad Tayyebi

- 16:30-16:50 Methods Used to Extract the Photovoltaic Cells and Panel Parameters
Adrian Marius Deaconu
- 16:50-17:10 Credentials are the holy grail for hackers
Cristina-Alexandra Căldărea, Silviu-Răzvan Dumitrescu
- 17:10-17:30 An incremental minimum flow algorithm
Luciana Majercsik
- 17:30-17:50 Bottleneck spanning tree interdiction problem with fixed and linear costs
Abdolahzadeh Abolfazl, Massoud Aman, Javad Tayyebi

17:50-18:00 Coffee Break

Chair: Aurelian Cernea

- 18:00-18:20 Spatial behaviour in the coupled theory of viscoelasticity of porous materials
Adina Chirilă
- 18:20-18:40 Existence of solutions for a variational relation problem
Dan Florin Serac
- 18:40-19:00 Some results for isotropic micropolar bodies with pores
Iana-Mihaela Fudulu and Marin Marin
- 19:00-19:20 Methods and mathematical models in stability or optimal control for dynamical systems
Mircea Lupu

19:30 Dinner ("Casa Romaneasca" Restaurant – Piața Unirii 15)

September 17, 2022

Chair: Silviu-Răzvan Dumitrescu

9:00-9:50 Plenary video session

9:00-9:50 Inside Neural Networks
Detlef Streitferdt

Room PIII1–Iuliu Maniu no.50

10:00-15:00 Excursion and Lunch

Departure from Faculty of Mathematics and Computer Science–*Iuliu Maniu no. 50*

And ... other participants of MACOS 2022:

Nicoleta Enache-David

Olivia Florea

Andreea Fulga

Gabriela Petrusel

Gabriel Stan

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PENTALOG

LIVEZILE DOBRINOIU

Abstracts

Combinatorial optimization interdiction problems with linear costs

Javad Tayyebi¹

¹Department of Industrial Engineering, Birjand University of Technology, Iran

September 15
16:00-16:50
Transilvania
University Hall

Abstract: A most important category of optimization problems is the class of combinatorial optimization (CO) problems. A CO problem constitutes two sets: a set E as well as a subset P of the power set of E . The elements of P are called objects and have a common structure depended on the problem. There is a decision maker, called the user, whose aim is to find an object which optimizes an objective function among all objects of P . Two types of objective functions are studied in the literature: (I) sum type (II) bottleneck type. Here, we investigate an extension of CO problems in which there is another decision maker except the user, called the attacker. Two decision makers have conflicting goals. The user wants to solve the CO problem while the attacker enables to change the coefficients of its objective function under some restrictions so as to worsen the optimal value of the user as much as possible. This problem is referred to as the combinatorial optimization interdiction (COI) problem. It is supposed that the attacker faces with two types of constraints: a linear budget constraint and bound constraints. We develop algorithms to show that the COI problem with linear interdiction costs can be solved in polynomial time for both the types of objective functions under some special circumstances.

Semilocal Approximation an some popular Diophantine equations

Preda Mihăilescu¹

¹ Mathematisches Institut, Georg-August-University,
Goettingen, Germany

September 15
17:10-18:40
Transilvania
University Hall

Abstract: We present new techniques of semilocal approximation of algebraic numbers emerging from the assumed solutions to some popular ternary exponential Diophantine equations.

Inevitable remarks on some recent results in metric fixed point theory

September 16
9:00-9:50
Transilvania
University Hall

Erdal Karapınar¹

¹ Cankaya University, Ankara, Turkey.

Abstract: The main goal of this talk is to express the dilemmas of the metric fixed point theorems that was initiated by Banach in 1922. It is quite possible to Express many of the real-world problems in the context of the fixed point theorems. It indicates that how the fixed point theory is useful and how huge application potential it has. But, a lot of results are repeated in this theory, which is of great interest. A substantial part of the new results suggested overlaps with the already existing results.

To support this observation, I shall share a few examples from the current literature.

Successive coefficients of close-to-convex functions

September 16
10:00-10:20

Paweł Zaprawa¹

¹ Lublin University of Technology, Poland

Abstract: Let \mathcal{C} denote the class of univalent functions which are close-to-convex in the unit disk Δ . A function f belongs to \mathcal{C} if there exist a number $\beta \in (-\pi/2, \pi/2)$ and a function $g \in \mathcal{S}^*$, starlike in Δ , such that

$$\left\{ \frac{e^{i\beta} z f'(z)}{g(z)} \right\} > 0, \quad z \in \Delta .$$

We consider a subclass $\mathcal{C}_0(k)$ of \mathcal{C} , for which $\beta = 0$ and a starlike function g is of the form $k(z) = \frac{z}{(1-z)^2}$. Functions in $\mathcal{C}_0(k)$ satisfy the following geometric condition

$$w \in f(\Delta) \Rightarrow \{w + t : t \geq 0\} \subset f(\Delta) .$$

This means that each function in $\mathcal{C}_0(k)$ is convex in the positive direction of the real axis.

Let $F_n = a_{n+1} - a_n$ and $G_n = |a_{n+1}| - |a_n|$. We obtain the estimates of $|F_n|$ and G_n , $n \in \mathbb{N}$ while $f \in \mathcal{C}_0(k)$.

On Marx-Strohhäcker type results for multivalent functions and their n^{th} root

Dorina Răducanu ¹

¹Transilvania University of Brasov, Romania

September 16
10:20-10:40
UI6 Room

Abstract: Two Marx-Strohhäcker type results for multivalent functions and their n^{th} root are given. Both results provide a lower bound, over the unit disc, of $\Re \sqrt[n]{\frac{f(z)}{z^p}}$ for functions that are p -valent starlike of a given order and uniformly p -valent starlike of a given order, respectively. Connections with previous results are indicated.

Logarithmic coefficients for a class of analytic functions defined by subordination

Andreea Nistor-Șerban¹ and Dorina Răducanu ²

¹Transilvania University of Brasov, Romania

²Transilvania University of Brasov, Romania

September 16
10:40-11:00
UI6 Room

Abstract: In this paper we consider a class of functions $\mathcal{M}_\alpha(\varphi)$ defined by subordination, consisting of functions $f \in \mathcal{A}$ satisfying the condition

$$(1 - \alpha) \frac{zf'(z)}{f(z)} + \alpha \left(1 + \frac{zf''(z)}{f'(z)} \right) \prec \varphi(z), \quad z \in U.$$

In the study of univalent functions, estimates on the Taylor coefficients are usually given. Another significant problem deals with the estimates of logarithmic coefficients. For the class \mathcal{S} of univalent functions no sharp bounds for the modulus of the individual logarithmic coefficients are known if $n \geq 3$. For different subclasses of \mathcal{S} the results are not better and in most cases only the first three initial coefficients of $\log \frac{f(z)}{z}$ are considered. For the class $\mathcal{M}_\alpha(\varphi)$ we obtain upper bounds for the logarithmic coefficients γ_n , $n \in \{1, 2, 3\}$ and also for Γ_n , $n \in \{1, 2, 3\}$, the logarithmic coefficients of the inverse of $\mathcal{M}_\alpha(\varphi)$. Connections with previous known results are pointed out.

Some new characterizations of inner product spaces regarding the p -angular distance

September 16
11:00-11:20
UI6 Room

Mario Krnić (joint work with Nicusor Minculete)¹

¹University of Zagreb, Croatia

Abstract: In this talk we derive some new bounds for the p -angular distance

$$\alpha_p[x, y] = \left\| \|x\|^{p-1}x - \|y\|^{p-1}y \right\|$$

in a normed linear space X and consequently, we establish the corresponding new characterizations of inner product spaces. Our first goal is to prove a characterization of an inner space which looks familiar to the Hile inequality, although it shows significantly different behavior since the Hile inequality holds in every normed space. More precisely, we prove that if $|p| \geq |q|$, $p \neq q$, then X is an inner product space if and only if for every $x, y \in X \setminus \{0\}$,

$$\alpha_p[x, y] \geq \frac{\|x\|^p + \|y\|^p}{\|x\|^q + \|y\|^q} \alpha_q[x, y].$$

Next, we establish several new characterizations of an inner space based on the Maigranda bounds for the angular distance. Finally, our results are compared with some previously known results from the literature.

Asymptotic expansions of stable means

September 16
11:30-11:50
UI6 Room

Lenka Mihoković¹

¹University of Zgreb, Croatia

Abstract: Consider *bivariate mean* M , i.e. function $M: \mathbb{R}^+ \times \mathbb{R}^+ \rightarrow \mathbb{R}^+$ such that

$$\min(a, b) \leq M(a, b) \leq \max(a, b).$$

M. Raissouli introduced a notion of *stable mean* with the following condition imposed

$$M(a, b) = M(M(a, M(a, b)), M(M(a, b), b)).$$

It can easily be seen that the arithmetic mean is stable and more general, the binomial power mean is also stable. The logarithmic and identric means are known not to be stable. The open problem of finding all pairs (p, q) such that Gini means $G_{p,q}$ and Stolarsky means $E_{p,q}$ are stable was stated by the same author.

The series $\sum_{n=0}^{\infty} a_n \varphi_n(x)$ is said to be an *asymptotic expansion* of a function $f(x)$ as $x \rightarrow x_0$ if for each $N \in \mathbb{N}$

$$f(x) = \sum_{n=0}^N a_n \varphi_n(x) + o(\varphi_N(x)).$$

Approximation of the function to a given accuracy is achieved by approaching the variable to a certain fixed point or a point at infinity. A small number of members of this series ensures a good approximation.

For a symmetric homogeneous stable mean we find asymptotic power series expansion of a form

$$M(x-t, x+t) = \sum_{n=0}^{\infty} a_n t^{2n} x^{-2n+1}, \text{ as } x \rightarrow \infty,$$

where coefficients a_n are given by recursive relation. By including known asymptotic expansions of parametric means it is shown how the obtained coefficients are used to solve the problem of identifying stable means within classes of parametric means under consideration.

Comparison of exact and heuristic method for numerical approximation of functions

Tomislav Burić¹

¹University of Zagreb, Croatia

September 16
11:50-12:10
UI6 Room

Abstract: We analyse and compare exact and heuristic methods for numerical evaluation of elementary functions in terms of polynomial and rational approximations. The results are presented together with advantages and disadvantages of exact methods in regard to heuristic methods considering function behaviour within interval for which approximation is obtained.

Redistributing algorithms and Shannon's Entropy: how to redistribute the ties?

Flavia-Corina Mitroi-Symeonidis¹ and Eleutherius Symeonidis²

¹Academy of Economic Studies, Department of Applied Mathematics,
Calea Dorobanți 15-17, sector 1, Bucharest RO-010552, Romania

²Mathematisch-Geographische Fakultät, Katholische Universität Eichstätt-Ingolstadt,
85071 Eichstätt, Germany

September 16
12:10-12:30
UI6 Room

Abstract: The mathematical problems discussed in our talk arise in the framework of time series analysis. The permutation entropy is used, and the underlying probabilities are established by redistributing the tuples with ties. We point out the changes of Shannon's entropy due to modifications of the distribution probability by means of various redistributing algorithms.

On the Space of Homogeneous Modified Harmonic Polynomials

September 16
12:30-12:50
UI6 Room

Eleutherius Symeonidis¹

¹Mathematisch-Geographische Fakultät, Katholische Universität Eichstätt-Ingolstadt,
85071 Eichstätt, Germany

Abstract: The solutions $u : \Omega \rightarrow \mathbb{R}$ (Ω a domain in \mathbb{R}^d , $d \geq 3$) of the equation

$$x_d \cdot \left(\frac{\partial^2 u}{\partial x_1^2} + \dots + \frac{\partial^2 u}{\partial x_d^2} \right) + (d-2) \cdot \frac{\partial u}{\partial x_d} = 0$$

are called *modified harmonic functions*. Let $r := \sqrt{x_1^2 + \dots + x_d^2}$. In his article entitled "Modified Spherical Harmonics in Several Dimensions" (Adv. Appl. Clifford Algebr., 29 (2019)), Heinz Leutwiler conjectures that the set

$$\left\{ r^{2n+2d-4} \cdot \frac{\partial^n r^{4-2d}}{\partial x_1^{\alpha_1} \dots \partial x_{d-1}^{\alpha_{d-1}}} \mid \alpha_1, \dots, \alpha_{d-1} \in \cup\{0\}; \alpha_1 + \dots + \alpha_{d-1} = n \right\}$$

is linearly independent, thus forming a basis of the space of homogeneous modified harmonic polynomials of degree n on \mathbb{R}^d . In our talk we present a proof of this conjecture.

Estimates of approximation using higher order moduli of continuity

September 16
12:50-13:10
UI6 Room

Radu Păltănea¹

¹Faculty of Mathematics and Computer Science,
Transilvania University of Braşov, Romania

Abstract: For a function $f \in B[a, b]$, for an integer $k \geq 2$ and for a number $h > 0$, we consider the following modulus of continuity of order k :

$$\tilde{\omega}_k(f, h) = k! \sup \left\{ \prod_{i=1}^k (x_{i+1} - x_i) |[f; x_1, x_2, \dots, x_{k+1}]|, \right. \\ \left. a \leq x_1 < x_2 < \dots < x_{k+1} \leq b, x_{k+1} - x_1 \leq kh \right\},$$

where $[f; x_1, x_2, \dots, x_{k+1}]$ is the divided difference of function f on the points $x_1 < x_2 < \dots < x_{k+1}$. Also denote by

$$\omega_j(f, h) = \sup \{ |\Delta_\rho f(x)|, x, x + \rho \in [a, b], 0 < \rho \leq h \},$$

the usual moduli of continuity of order $j \geq 1$.

Let $L : C[a, b] \rightarrow C[a, b]$ be an arbitrary positive linear operator. We obtain a general estimate of the difference $|L(f, x) - f(x)|$, $x \in [a, b]$, using modulus $\tilde{\omega}_k(f, h)$ in combinations with the moduli of continuity $\omega_j(f, h)$, $1 \leq j \leq k-1$ in terms of the moments of operator L .

In the second part it is obtained a general estimate of the degree of approximation for arbitrary positive linear operators using a double weighted second order modulus of continuity.

Several inequalities related to the numerical radius

Nicușor Minculete¹

¹Faculty of Mathematics and Computer Science,
Transilvania University of Brașov, Romania

September 16
13:10-13:30
UI6 Room

Abstract: The aim of this presentation is to give new upper bounds of $\omega(T)$, which denotes the numerical radius of an operator T on a Hilbert space $(H, \langle \cdot, \cdot \rangle)$. Next, we give certain inequalities about radius $\omega(S^*T)$.

Energy drift and stochastic process in the three-body problem

Marian Gîdea¹

¹Yeshiva University, New York, USA

September 16
15:30-16:20
Transilvaniay
University Hall

Abstract: We consider the three-body problem as a model for the motion of a small body (e.g., asteroid or spacecraft) under the gravitational influence of two massive bodies (e.g., Sun and Jupiter). We study the effect of the eccentricity of the orbits of the massive bodies on the motion of the small body. We show that for all small eccentricity values we can find trajectories of the asteroid along which the energy can grow significantly. Also, we can find trajectories which make chaotic jumps in energy. We show that the distributions of energies along such trajectories converge to a Brownian motion with drift as the eccentricity value tends to zero. Our results solve some conjectures made by V.I. Arnold and B. Chirikov. We use a methodology that combines geometric and topological methods with computer assisted proofs.

About some speeds of convergence to the the constant of Euler

Andrei Vernescu¹

¹Valahia University of Târgoviște, Romania

September 16
16:30-16:50
UI6 Room

Abstract: The speed of convergence of the classical sequence which defines the constant of Euler (or Euler- Mascheroni), $\gamma = \lim_{n \rightarrow \infty} \gamma_n = 0.5777\dots$, where

$$\gamma_n = \sum_{k=1}^n \left(\frac{1}{k} \right) - \ln n, \text{ was intensively studied.}$$

In 1983, I established one of the first two sided estimates of this speed, namely $\frac{1}{2n+1} < \gamma_n - \gamma < \frac{1}{2n}$. Further several new sequences with a faster convergence are defined either by modifying the argument of the logarithm (De Temple, 1993, Negoii 1997, Ivan 2002) or by modifying the last term $1/n$ of the harmonic sum (Vernescu 1999). Now we give a systematic study of these speeds of convergence and especially of the last ones.

On approximation properties of some non-positive Bernstein-Durrmeyer type operators modified in the Bezier-King sense

September 16
16:50-17:10
UI6 Room

Bianca Vasian¹

¹Faculty of Mathematics and Computer Science,
Transilvania University of Braşov, Romania

Abstract: In this paper we will propose some new Bernstein-Durrmeyer type operators modified in Bezier-King sense, which are not positive on the entire interval $[0, 1]$. Firstly we will show that these operators approximate all continuous functions on an interval $[0, \xi]$ on which they are positive, using the Ditzian-Totik modulus of continuity. Further, we will prove that, even though the operators are not positive on the entire $[0, 1]$, they can approximate all continuous functions on $[0, 1]$, first, by using the first order modulus of continuity, and then the second order one, with the appropriate K -functionals

On the convergence of power series of positive linear operators

September 16
17:10-17:30
UI6 Room

Ştefan Garoiu¹ and Radu Păltănea²

^{1,2}Faculty of Mathematics and Computer Science,
Transilvania University of Braşov, Romania

Abstract: In this paper we will introduce a more general series of Bernstein operators which will be an extension of geometric series of Bernstein operators introduced by R. Păltănea. Namely, we will introduce the operators $A_n^s : \psi C[0, 1] \rightarrow \psi C[0, 1]$, given by $A_n^s = \frac{1}{s!n^{s+1}} \sum_{k=s}^{\infty} (k)_s (B_n)^{k-s}$, where $(k)_s = k(k-1)\dots(k-s+1)$ and we will study their approximation properties. In this sense, we have obtained a convergence result and a generalized Voronovskaja theorem. On the other hand, following the work of Raşa, we will prove that our operator approximate the integral of the C_0 -semigroup approximated by Bernstein operators, mentioning that our proof relies on applying Nachbin's theorem instead of using the eigenvalues of Bernstein operators. We mention that these results can be extended to a more general class of operators on the space $C_0[0, 1]$, but this would require too many additional conditions, therefore we will restrict ourselves only to Bernstein operators.

The 3-convexity flavor of the Hornich-Hlawka inequality

Constantin P. Niculescu^{1,2}

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²Academy of Romanian Scientists, Bucharest, Romania

September 16
17:30-17:50
UI6 Room

Abstract: The following result is proved:

Suppose that E is an ordered Banach space and $f : \mathbb{R}_+ \rightarrow E$ is a continuous 3-convex function. Then f verifies the functional inequality

$$f(x) + f(y) + f(z) + f(x + y + z) \geq f(x + y) + f(y + z) + f(z + x) + f(0)$$

for all $x, y, z \in \mathbb{R}$.

If, in addition, f is nondecreasing and concave, then

$$f(|x|) + f(|y|) + f(|z|) + f(|x + y + z|) \geq f(|x + y|) + f(|y + z|) + f(|z + x|) + f(0)$$

for all $x, y, z \in \mathbb{R}$.

This extends a result previously obtained by Ressel by a different method.

End-to-end data privacy using homomorphic encryption models

Răzvan Bocu¹ and Delia Monica Duca Iliescu²

^{1,2}Faculty of Mathematics and Computer Science,
Transilvania University of Braşov, Romania

September 16
18:00-18:20
UI6 Room

Abstract: The integrated collection of personal health data represents a relevant research topic, which is enhanced further by the development of next-generation mobile networks that can be used in order to transport the acquired medical data. The gathering of personal health data has become recently feasible using relevant wearable personal devices. Nevertheless, these devices do not possess sufficient computational power, and do not offer proper local data storage capabilities. This paper presents an integrated personal health metrics data management system, which considers a virtualized symmetric 5G data transportation system. The personal health data are acquired using a client application component, which is normally deployed on the user's mobile device, regardless if it is a smartphone, smartwatch, or another kind of personal mobile device. The collected data are securely transported to the cloud data processing components, using a virtualized 5G infrastructure and homomorphically encrypted data packages. The system has been comprehensively assessed through the consideration of a real-world use case, which is presented.

Mammographic texture analysis in the diagnosis of breast cancer

September 16
18:20-18:40
UI6 Room

Andreea-Bianca Lixandru¹, Laura Dioşan² and Mircea-Lucian Sasu³

¹ Transilvania University of Brasov, Romania

² University Babeş-Bolyai, Cluj-Napoca, Romania

³ Transilvania University of Brasov, Romania

Abstract: Worldwide, the incidence of breast cancer is expanding. Although population-based screening is accessible in many nations, it may not be the best use of digitalization resources. The adoption of a solution based on automatic processing of mammographies is a crucial component of risk-based screening. In this paper we investigate multiple models for classification of textures on a medical dataset which contains mammography scans. For extracting the features, in this article we will present two different approaches: one will use the Local Binary Pattern feature and the other one will use the Gray Level Co-occurrence Matrix feature, to make possible a texture classification for MIAS dataset. More than this, the models are validated on Kylberg dataset and we observed that the classification using texture features is working very promising also on the medical dataset. The research will present in detail the implementation, the scores obtained for both approaches and a comparison between the models.

Advances in CUDA for Computational Physics

September 16
18:40-19:00
UI6 Room

Delia Spridon¹

¹Faculty of Mathematics and Computer Science,
Transilvania University of Braşov, Romania

Abstract: Advances in the GPU development led to the opportunity for software developers to increase the execution speed for their programs by massive parallelization of the algorithms by using GPU programming. CUDA is a parallel computing architecture developed by NVIDIA and it includes a set of CUDA instructions and the hardware part for parallel computing. Computational Physics is an interdisciplinary field in continuous development that studies, develops and optimizes numerical algorithms and computational techniques for their application in solving various physics problems. Computational Physics has applicability in all sub-branches of physics or similar fields: biophysics, astrophysics, plasma physics, biomechanics, fluid physics, etc. Moreover, with the evolution of technology in the last few decades, this relatively new field has helped to quickly obtain results in these fields, facilitating the connection between theoretical and experimental physics. In this paper, the latest researches and results obtained in computational physics, especially in plasma domain by using GPU computing with CUDA architecture are presented.

**Image processing in medicine: the algorithms and datasets
for searching
the spatial location of brain intracranial aneurysms**

Sergey Sinitza¹

¹Kuban State University, Krasnodar, Russia

September 16
19:00-19:20
UI6 Room

Abstract: This presentation is about the current results of solving the problem of cerebral aneurysms spatial location according to computer tomography and magnetic resonance imaging angiography data. It also gives a review of algorithms and datasets that can be used to perform this search.

Fixed Point Theory for Abstract Volterra Operators

Adrian Petrușel¹

¹Babeș-Bolyai University, Department of Mathematics, Cluj-Napoca, Romania

September 16
10:00-10:20
UI3 Room

Abstract: Several notions of abstract Volterra operators on spaces of functions of one variable are well known (C. Corduneanu, Abstract Volterra equations: a survey, Math. Comput. Modeling, 32(2000), 1503-1528; E.S. Zhukovskii, M.J. Alves, Abstract Volterra operators, Russian Math., 52(2008), 1-14; I.A. Rus, Some variants of contraction principle in the case of operators with Volterra property: step by step contraction principle, Adv. Theory of Nonlinear Anal. Appl., 3(2019), No. 3, 111-120). In this paper, we introduce a notion of abstract Volterra operators in spaces of functions of several variables. Some fixed point equations with such abstract Volterra operators are also studied. The talk is based on a recent joint work with I.A. Rus.

Interpolation type iterated function systems

Radu Miculescu¹

¹Transilvania University of Brașov,
Faculty of Mathematics and Computer Science, Brașov, Romania

September 16
10:20-10:40
UI3 Room

Abstract: By scrutinizing the crucial features of the iterated function systems used in the construction of fractal interpolation functions we introduce the concept of interpolation type iterated function system and prove that such a system has attractor and that it admits canonical projection.

September 16
10:40-11:00
UI3 Room

Fixed points of interpolative contractions

Isa Yildirim¹, Y. Serdar Sahin²

¹Atatürk University, Turkey

²Atatürk University, Turkey

Abstract: The purpose of this paper is to give some results for classes of interpolative Kannan type contraction and interpolative Reich–Rus–Cirić type contraction in complete convex b -metric spaces (in short ccbms).

September 16
11:00-11:20
UI3 Room

A countable fractal interpolation scheme involving Rakotch contractions

Cristina Păcurar¹

¹Faculty of Mathematics and Computer Science,
Transilvania University of Braşov, Romania

Abstract: The main result of this paper states that for a given countable system of data Δ , there exists a countable iterated function system consisting of Rakotch contractions, such that its attractor is the graph of a fractal interpolation function corresponding to Δ . In this way, on the one hand, we generalize a result due to N. Secelean (see *The fractal interpolation for countable systems of data*, Univ. Beograd. Publ. Elektrotehn. Fak. Ser. Mat., **14** (2003), 11–19) by considering countable systems consisting of Rakotch contractions rather than Banach contractions. On the other hand, we generalize a result due to S. Ri (see *A new idea to construct the fractal interpolation function*, Indag. Math., **29** (2018), 962-971) by considering countable (rather than finite) systems consisting of Rakotch contractions. Some exemplifications are provided.

September 16
11:30-11:50
UI3 Room

Some remarks on convex orbital operators

Ovidiu Popescu¹

¹Transilvania University of Braşov, Department of Mathematics and Computer Sciences,
Braşov, Romania

Abstract: The aim of this paper is to clarify the notion of orbital convex Lipschitz operator and prove some fixed point theorems which generalize and complement several results in the theory of nonlinear operators.

The approximation of controls using moment problems

Ionel Roventța¹ and József Kolumbán²

¹Department of Mathematics, University of Craiova, Romania

September 16
11:50-12:10
UI3 Room

Abstract: We consider a finite-difference semi-discrete scheme for the approximation of boundary controls for wave equation. The continuous problem is controllable but the high frequency numerical spurious oscillations lead to a loss of the uniform (with respect to the mesh size) controllability property of the semi-discrete model in the natural setting.

Basically, this difficulty can be treated using an appropriate filtering technique to eliminate the short wave length components of the solutions/initial data of the discrete system, i.e. the large frequencies of the discretized problem. Our aim consists of filtering the initial data in an optimal range in order to restore the uniform controllability property. Moreover, we obtain a relation between the range of filtration and the minimal time of control. The technique used here is based on solving a moment problem.

A study on the Research Directions of some Cesàro and Rhaly Operators

Amelia Bucur¹, María del Carmen Listán - García² and María del Pilar Romero-De La Rosa³

September 16
12:10-12:30
UI3 Room

¹Lucian Blaga University of Sibiu, Romania

²University of Cádiz, Spain

³University of Cádiz, Spain

Abstract: In this article, we present a study on the research directions for Cesàro operators and their generalizations, with details for two different directions, namely (A) extended eigenvalues and extended eigenoperators, and (B) statistical convergence and strong Rhaly convergence. Thus, one of the purposes of this paper is to give an observation of the extended eigenvalues to the third power of the discrete Cesàro operator C_0 defined on the complex Banach spaces l^2 by the expression

$(C_0 f)(n) = \frac{1}{n+1} \sum_{k=0}^n f(k)$. For a bounded linear operator T on a complex Banach

space, a complex scalar λ is said to be an extended eigenvalue, if there is a non-zero operator X and $TX = \lambda XT$. Such an operator X is called an extended eigenoperator of T corresponding to the extended eigenvalue λ . In this work it is shown that the set of extended eigenvalues for the operator $C_0^3 : l^2 \rightarrow l^2$, is the interval $[1, \infty)$. Also, for one of the generalizations of the discrete operator Cesàro, namely a type

of Rhaly operators, $(R_a f)(n) = \frac{1}{a_n} \sum_{k=0}^n f(k)$, we presented details about statistical

convergence and strong Rhaly convergence by moduli for double sequences. Given a modulus function f , we established that a double sequence that is f -strong Rhaly convergent is always f -statistically convergent. The results of this paper adapt the

Fixed point theory for multi-valued nonlinear graph contractions in complete metric spaces

September 16
12:30-12:50
UI3 Room

Mădălina Moga¹, Adrian Petrușel², Radu Trușcă³

¹Babeș-Bolyai University Cluj-Napoca, Romania

²Academy of Romanian Scientists, Romania

³Babeș-Bolyai University Cluj-Napoca, Romania

Abstract: Let (M, d) be a metric space and $P(M)$ be the set of all nonempty subsets of M . We also denote by $P_{cl}(M)$ the set of all nonempty closed subsets of M . We denote by H the generalized Pompeiu-Hausdorff metric on $P_{cl}(M)$.

A function $\varphi : [0, \infty[\rightarrow [0, \infty[$ is called a strong comparison function if φ is increasing and the series $\sum_{k=0}^{\infty} \varphi^k(t)$ is convergent for any $t > 0$.

If $F : M \rightarrow P(M)$ is a multi-valued operator, then $m \in M$ is called a fixed point for F if $m \in F(m)$. Then, $Fix(F) := \{m \in M : m \in F(m)\}$ is the fixed point set of f , while the symbol $SFix(F) := \{m \in M : F(m) = \{m\}\}$ denotes the set of all strict fixed points of F . The symbol $Graph(F) := \{(m, p) \in M \times M : p \in F(m)\}$ is the graph of the multi-valued operator F .

Definition. Let (M, d) be a metric space. Then, an operator $F : M \rightarrow P(M)$ is called a multi-valued graph φ -contraction if there exists a strong comparison function $\varphi : [0, \infty[\rightarrow [0, \infty[$ such that

$$H(F(m), F(p)) \leq \varphi(d(m, p)), \text{ for every } (m, p) \in Graph(F).$$

The purpose of this paper is to give several results, concerning existence, approximation and localization of the fixed point/strict fixed points, for the fixed point inclusion $m \in F(m)$ where $F : M \rightarrow P_{cl}(M)$ is a multi-valued nonlinear graph φ -contraction.

Some fixed point theorems in the framework of f -metric spaces

September 16
12:50-13:10
UI3 Room

Bogdan-Cristian Anghelina¹

¹Faculty of Mathematics and Computer Science,
Transilvania University of Brașov, Romania

Abstract: This presentation is concerned with the notion of f -metric space, a genuine generalization of the concept of b -metric space. We extend Matkowski, Kannan and Chatterjea type fixed point theorems in the context of f -metric spaces.

φ – Contractive Orbital Affine Iterated Function Systems

Irina Savu¹

¹University Politehnica of Bucharest, Faculty of Applied Sciences, Bucharest, Romania

September 16
13:10-13:30
UI3 Room

Abstract: In this paper we introduce the notion of φ –contractive orbital affine iterated function system (oAIFS for short), which is based on the notions of affine iterated function system and φ –contractive orbital iterated function system. We present two results which give a description of the functions of an oAIFS and establish sufficient conditions to exist a norm with specific properties on the linear space where the functions are defined. Two examples are provided.

An application of Edelstein’s contraction principle: the attractor of a graph-directed generalized iterated function system

Radu Miculescu¹, Alexandru Mihail² and Silviu-Aurelian Urziceanu

¹Transilvania University of Brasov, Romania

²University of Bucharest, Romania

³Polytechnic University of Bucharest, Romania

September 16
16:30-16:50
UI3 Room

Abstract: This paper gathers two generalizations of iterated function systems, namely the one introduced by the first two authors under the name of generalized iterated function systems and the one introduced by D. Mauldin, S. Williams and G. Boore, K. Falconer under the label of graph-directed iterated function systems. By combining them we introduce the concept of a graph-directed Generalized iterated function system. We prove that, under suitable contractivity assumptions on the constitutive functions of such a system and structural assumptions on the underlying metric space, it generates, via Edelstein’s contraction principle, a unique attractor. The result is illustrated by two examples.

About the B-concavity of functions with many variables

Alexandra-Diana Melesteu¹

¹Transilvania University of Brasov, Faculty of Mathematics and Informatics, Romania

September 16
16:50-17:10
UI3 Room

Abstract: The paper deals with the study of the property of B-concavity and BB-concavity in the multi-dimensional case and with the relation between these properties and the Bernstein operators defined on a simplex.

September 16
17:10-17:30
UI3 Room

Fixed point theorems on product of b -metric spaces

Izabella Abraham¹

¹Faculty of Mathematics and Computer Science,
Transilvania University of Braşov, Romania

Abstract: The aim of this paper is to extend some fixed point results from [Şerban, M. A., *Teoria punctului fix pentru operatori definiți pe produs cartezian*, Presa Universitară Clujeană, Cluj–Napoca, 2002] and [Prešić, S. B., *Sur une classe d'inéquations aux différences finite et sur la convergence de certaines suites*, Publ. Inst. Math. (Beograd) (N. S.). **5(19)** (1965), 75-78] in the framework of b -metric spaces.

September 16
10:00-10:20
UI2 Room

On the solutions of several coupled systems of fractional differential inclusions

Aurelian Cernea¹

¹Faculty of Mathematics and Informatics, University of Bucharest, Romania

Abstract: We present a short survey of some recent results concerning the existence of solutions for several classes of coupled systems of fractional differential inclusions. Such kinds of coupled systems seem to be very useful in the research of several physical phenomena.

We consider systems with integro-multistrip-multipoint boundary conditions, with nonlocal non-separated boundary conditions, with mixed order fractional order differential inclusions and with nonlocal integral boundary conditions

Our approach use Filippov's technique, avoids the applications of fixed point theorems and takes into account the case when the values of the set-valued maps are not convex; instead the set-valued maps are assumed to be Lipschitz in the second and third variable..

September 16
10:20-10:40
UI2 Room

Fractional q -difference Schrödinger equations with integral and multi-point boundary conditions

Umit Aksoy¹

¹Atılım University, Turkey

Abstract: In this talk, we study the existence and uniqueness of the solution of a class of nonlinear fractional q -difference Schrödinger equations with integral and multi-point boundary conditions. We introduce the Green's function for the associated linear problem which is used to transform the nonlinear problem into an integral equation. Conditions for the existence-uniqueness of the solution of the problem are discussed and an example is provided to demonstrate the application of our result.

Tudor Barbu¹

¹Faculty of Mathematics and Computer Science,
Transilvania University of Braşov, Romania

Abstract: Edge detection, which has the purpose of detecting sharp changes in image brightness, represents a fundamental tool in image processing and analysis, and computer vision. It includes a variety of mathematical approaches that aim at identifying the edges in digital images. Here, the state of the art edge detection techniques based on partial differential equations (PDE) are surveyed. Our own contributions in this image analysis domain are also presented in this work. The anisotropic diffusion-based edge detection techniques inspired by the influential Perona – Malik diffusion model are discussed first. Nonlinear reaction-diffusion models for edge detection are then presented here. One of them uses a modified version of the Perona – Malik scheme with edge indicators, while another one is based on a modified version of the FitzHugh-Nagumo reaction-diffusion equations. Another image edge detection solution described here combines successfully anisotropic diffusion and total variation-based models. Other variational edge detection algorithms based on the total variation (TV) regularization are also described. A nonlinear diffusion-based edge detection approach using the mean curvature motion and a local scale controlled piecewise linear diffusion model for edge detection are discussed next. Fuzzy anisotropic diffusion-based edge detection algorithms are also presented. Nonlinear PDE-based detection techniques using higher order partial differential equations, such as the fourth-order You-Kaveh model, or combinations between second and fourth order PDEs, are then described. Finally, the edge detection techniques developed by us are presented in this work. While the most of the anisotropic diffusion-based edge detection schemes have a variational character, the nonlinear PDE-based models proposed by us are non-variational, since they cannot be derived from some energy functional minimizations. Such an effective automatic edge detection method that is described here performs a nonlinear anisotropic diffusion-based multi-scale image analysis by using a non-variational well-posed second-order PDE model. The edges are detected at each scale of this PDE-based scale-space by determining the zero-crossings and applying some gradient magnitude thresholding operations and morphological processes. The edges identified at multiple scales are then combined using a fine-to-coarse edge tracking approach. Method comparison results are also provided. .

On the existence and uniqueness of solutions of fractional dynamic equations on time scales

September 16
11:00-11:20
UI2 Room

Inci Erhan¹

¹Atılım University, Turkey

Abstract: In this talk, we discuss the existence and uniqueness of solutions of a Cauchy problem associated with a nonlinear Caputo fractional dynamic equation of arbitrary order $\alpha > 0$, defined on a time scale. After detailed introduction on the fractional integral and derivatives on time scales, we state the problem and formulate it as a fixed point problem posed on a b -metric space. Finally, we present a numerical example to support our theoretical results.

On the Mersenne Hybrinomial Quaternions

September 16
11:30-11:50
UI2 Room

Engin Özkan¹, Bahar Kuloğlu² and Engin Eser³

^{1,2,3}Erzincan Binali Yıldırım University, Turkey

Abstract: In this paper, we introduce Mersenne hybrinomial quaternions and present some of their properties. Some identities are derived for these polynomials. Furthermore, we give the Binet formulas, Catalan, Cassini, d'Ocagne identity and generating and exponential generating function of these hybrinomial quaternions.

On Mersenne Hybrid Quaternions

September 16
11:50-12:10
UI2 Room

Engin Özkan¹ and Mine Uysal²

^{1,2}Erzincan Binali Yıldırım University, Turkey

Abstract: We define Mersenne, Mersenne-Lucas hybrid quaternion. We give the Binet's formula, the generating functions, exponential generating functions and sum formula of these numbers. We find some relations among Mersenne-Lucas hybrid quaternion, Jacobsthal hybrid quaternion, Jacobsthal-Lucas hybrid quaternion and Mersenne hybrid quaternion. Then we present some important identities such as Cassini identities for Mersenne, Mersenne-Lucas hybrid quaternion.

Division quaternion algebras over extensions of degree l^n (where l is an odd prime integer) of quadratic number fields

Diana Savin (joint work with Vincenzo Acciaro, Mohammed Taous and Abdelkader Zekhnini) ¹

September 16
12:10-12:30
UI2 Room

¹ Transilvania University of Brasov, Romania

Abstract: Let F be a quadratic number field and let p and q are positive prime integers. We obtain a complete characterization of division quaternion algebras $H_L(p, q)$, where L is an extension of F of degree l such that L is a dihedral extension of \mathbb{Q} , or else L is an abelian l -extension of F , unramified over F whenever l divides the class number of F .

Keywords: quaternion algebras; ramification theory in algebraic number fields.

MSC 2020: Primary: 11R04; 11R11; 11R21; 11R32: 11R52 ; 11S15; Secondary: 11R37; 11R29; 11A41; 11F85.

Surfaces associated with Pascal and Catalan triangles

Adela Mihai^{1,2}

¹Technical University of Civil Engineering Bucharest, Romania

²Transilvania University of Braşov, Romania

September 16
12:30-12:50
UI2 Room

Abstract: An open problem in reliability theory is that of finding all the coefficients of the reliability polynomial associated with particular networks. Because reliability polynomials can be expressed in Bernstein form (hence linked to binomial coefficients), it is clear that an extension of the classical discrete Pascal's triangle (comprising all the binomial coefficients) to a continuous version (exhibiting infinitely many values in between the binomial coefficients) might be geometrically helpful and revealing. We investigated some geometric properties of a continuous extension of Pascal's triangle: Gauss curvature, mean curvatures, geodesics and level curves, as well as their symmetries. These results have been published in [V. Beiu, L. Daus, M. Jianu, A. Mihai, I. Mihai, On a surfaces associated with Pascal's triangle, *Symmetry* 14(2) (2022), art. 411.]. As a further study, we investigate surfaces associated with Catalan triangles [S. Achimescu, L. Daus, M. Jianu, I. Mierlus-Mazilu, A. Mihai, D. Tudor, O.-A. Roman, On a surface associated to Catalan triangle, preprint].

September 16
12:50-13:10
UI2 Room

Cosmological Finsler Spacetimes

Nicoleta Voicu¹, Manuel Hohmann² and Christian Pfeifer³

¹Transilvania University of Braşov, Romania

²University of Tartu, Estonia

³Center of Applied Space Technology and Microgravity (ZARM), University of Bremen, Germany

Abstract: We first introduce the notion of Finsler spacetime manifold. Then, for Finsler spacetimes equipped with a global time function, we identify the Lie Algebra of symmetry generators of spatially homogeneous and isotropic Finsler geometries, thus generalizing Friedmann-Lemaître-Robertson-Walker geometry. In particular, we find the most general spatially homogeneous and isotropic Berwald spacetimes, which are Finsler spacetimes that can be regarded as closest to pseudo-Riemannian geometry.

September 16
16:30-16:50
UI2 Room

Methods Used to Extract the Photovoltaic Cells and Panel Parameters

Adrian-Marius Deaconu¹

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Transilvania University of Braşov, Romania

Abstract: The methods to estimate the parameters of the photovoltaic cells and panels have been developed since 1963. In time, the researchers developed methods to calculate one, two, and all parameters of the photovoltaic cells and panels, under different conditions, such as laboratory or natural sunlight conditions, under light or in the dark, in normal light, or in concentrated light. More recently, the meta-heuristic algorithms started to be used to extract the parameters of the photovoltaic cells and panels with very good accuracy. Nowadays, these algorithms surpass the other methods developed to calculate the photovoltaic cells parameters. This paper briefly presents the main methods introduced in time, and tested for photovoltaic parameters extraction. The algorithms' results for known datasets from literature are compared and ranked by different error formulae.

Credentials are the holy grail for hackers

Cristina-Alexandra Caldarea¹, Silviu-Razvan Dumitrescu²

September 16
16:50-17:10
UI2 Room

¹ Atos, Romania

² Transilvania University of Brasov, Romania

Abstract: Identity and Access Management is that module of Cyber Security domain which transforms identities into accounts. With an account you can authenticate to an application (ex: account provides credentials). To manage access on various features of the application you must have rights (permissions). This presentation will cover the general concept, some experienced good practices and what means innovation in IAM.

An Incremental Minimum Flow Algorithm

Luciana Majercsik¹

¹Transilvania University of Brasov, Romania

September 16
17:10-17:30
UI2 Room

Abstract: There are certain problems, that occur in economy, in the design of the electrical or water supply networks or in other various situations, that can be modelled and solved as minimum flow problems. When changes occur in the networks, either by the modification of the capacity or of the lower bound of an arc, the recalculation of the minimum flow in the modified network can be highly time consuming. This paper proposes an incremental minimum flow algorithm, based on a data structure that produces decreasing paths without complex computations.

Bottleneck spanning tree interdiction problem with fixed and linear costs

Abolfazl Abdolazadeh¹, Massoud Aman², Javad Tayyebi³

^{1,2,3}Department of Industrial Engineering, Birjand University of Technology, Iran

September 16
17:30-17:50
UI2 Room

Abstract: This paper investigates the bottleneck spanning tree interdiction problem. This is a game containing two players with conflicting goals. The first player, called the user, wants to find a bottleneck (min-max or max-min) spanning tree in a weighted network. The other player, called the attacker, increases edge weights under a budget constraint as well as bound constraints so that the user does not achieve his/her goal. This game has a hierarchy structure. It means that the attacker first perturbs the network and then, the user chooses his/her strategy after observing the attacker's action. This paper considers the problem in two cases that there are fixed and linear costs for the attacker. Two divide-and-conquer algorithms are developed to solve the problem under both the costs in polynomial time.

Spatial behaviour in the coupled theory of viscoelasticity of porous materials

September 16
18:00-18:20
UI2 Room

Adina Chirilă¹

¹Transilvania University of Brasov, Faculty of Mathematics and Informatics, Romania

Abstract: We analyse a right cylinder made of a viscoelastic material with pores. The mathematical model is represented by a system of equations of steady vibrations for the displacement vector, the changes of the volume fraction and the pressure. The spatial behaviour is characterised in terms of some cross-sectional functional.

Existence of solutions for a variational relation problem

September 16
18:20-18:40
UI2 Room

Mircea Balaj¹ and Dan Florin Serac²

^{1,2} University of Oradea, Romania

Abstract: Let X be a nonempty compact and convex subset of a topological vector space and Z be a topological vector space. Let $T : X \rightrightarrows Z$ be a set-valued mapping with nonempty, compact and convex values and $\rho(x, y, z)$ be a relation linking elements $x \in X$, $y \in X$ and $z \in T(X)$. Assume that:

- (i) ρ is T -convex in the variable z and closed.
- (ii) ρ^c is convex in the variable y ;
- (iii) ρ is T-KKM;

Then, there exists an $x_0 \in X$ and $z_0 \in T(x_0)$ such that $\rho(x_0, y, z_0)$ holds for all $y \in X$.

Some results for isotropic micropolar bodies with pores

September 16
18:40-19:00
UI2 Room

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Abstract: This paper is concerned with the theory of isotropic micropolar media, and its purpose is defined by obtaining both the variational principle and the continuous dependence in the case of the mentioned theory. An new presentation of our mixed problem is defined by the corresponding basic equations of the present theory and the initial and boundary conditions. With respect to this alternative characterization, the convolutional variational principle is obtained, followed by the obtaining of the continuous dependence of the solutions over the initial data and the terms of external supply in the present context.

Inside Neural Networks

Detlef Streitferdt¹

¹Technische Universität Ilmenau, Germany

September 17
9:00-9:50
PIII1 Room

Abstract: Machine learning became a prominent technology with artificial neural networks as its current and highly discussed model. Although the results of image analysis / recognition or speech detection are very promising, the analysis of neural networks itself and their behavior is still a very hard task due to the complexity of the models. Even a single software neuron puts high demands on the assessment of software quality aspects. Current models with thousands of interconnected neurons require by far more elaborated software tools and methods. This talk gives a software engineering overview of the current state in analyzing neural networks within the software development life-cycle. It addresses the limits of using neural networks and emphasizes the corresponding pitfalls a software engineer has to cope with.

Author Index

- Ștefan Garoiu, 16
- Abdelkader Zekhnini, 27
Abolfazl Abdolazadeh, 29
Adela Mihai, 27
Adina Chirilă, 30
Adrian Petrușel, 19, 22
Adrian-Marius Deaconu, 28
Alexandra-Diana Melesteu, 23
Alexandru Mihail, 23
Amelia Bucur, 21
Andreea Nistor-Șerban, 11
Andreea-Bianca Lixandru, 18
Andrei Vernescu, 15
Aurelian Cernea, 24
- Bahar Kuloğlu, 26
Bianca Vasian, 16
Bogdan-Cristian Anghelina, 22
- Christian Pfeifer, 28
Constantin P. Niculescu, 17
Cristina Maria Păcurar, 20
Cristina-Alexandra Caldarea, 29
- Dan Florin Serac, 30
Delia Monica Duca Iliescu, 17
Delia Spridon, 18
Detlef Streitferdt, 31
Diana Savin, 27
Dorina Răducanu1, 11
Dorina Răducanu2, 11
- Eleutherius Symeonidis, 13, 14
Engin Özkan, 26
Engin Eser, 26
Erdal Karapınar, 10
- Flavia-Corina Mitroi-Symeonidis, 13
- Iana M. Fudulu, 30
Inci Erhan, 26
Ionel Rovența, 21
Irina Savu, 23
Isa Yildirim, 20
Izabella Abraham, 24
- József Kolumbán, 21
Javad Tayyebi, 9, 29
- Laura Dioșan, 18
Lenka Mihoković, 12
Luciana Majercsik, 29
- Mădălina Moga, 22
Manuel Hohmann, 28
María del Carmen Listán-García, 21
María del Pilar Romero-De La Rosa,
21
Marian Gîdea, 15
Marin Marin, 30
Mario Krnić, 12
Massoud Aman, 29
Mine Uysal, 26
Mircea Balaj, 30
Mircea-Lucian Sasu, 18
Mohammed Taous, 27
- Nicoleta Voicu, 28
Nicușor Minculete, 15
- Ovidiu Popescu, 20
- Paweł Zaprawa, 10
Preda Mihăilescu, 9
- Răzvan Bocu, 17
Radu Miculescu, 19, 23
Radu Păltănea, 14, 16

Radu Trușc̃, 22

Sergey Sinita, 19

Silviu-Aurelian Urziceanu, 23

Silviu-Razvan Dumitrescu, 29

Tomislav Burić, 13

Tudor Barbu, 25

Umit Aksoy, 24

Vincenzo Acciario, 27

Y. Serdar Sahin, 20